

<b>PROFESSOR'S NAME</b>	Prof.M. Ramakrishna
<b>DEPARTMENT</b>	Department of Aerospace Engineering
<b>INSTITUTE</b>	Indian Institute of Technology Madras
<b>COURSE OUTLINE</b>	Representation of mathematical ideas on the computer: numbers, functions, derivative, differential equations. Simple problems: Solution to Laplace's equation, one-dimensional first order wave equation, heat equation, Finite difference schemes - stability and consistency, dissipation dispersion, finite volume method. One-dimensional Euler's equation: Discretisation, Delta form, application of boundary conditions. Advanced topics: Roe's averaging, Multigrid Methods, SOR and variational techniques.

### COURSE DETAILS

S. No	Module ID/ Lecture ID	Lecture Title/Topic
1.	L1	Introduction, Why and How We Need Computers
2.	L2	Representing Arrays and Functions on Computers
3.	L3	Representing Functions - Box Functions
4.	L4	Representing Functions - Polynomials & Hat Functions
5.	L5	Hat Functions, Quadratic & Cubic Representations
6.	L6	Demo - Hat Functions, Aliasing
7.	L7	Representing Derivatives - Finite Differences
8.	L8	Finite Differences, Laplace Equation
9.	L9	Laplace Equation - Jacobi Iterations

10.	L10	Laplace Equation - Iteration Matrices
11.	L11	Laplace Equation - Convergence Rate
12.	L12	Laplace Equation - Convergence Rate (Continued)
13.	L13	Demo - Representation Error, Laplace Equation
14.	L14	Demo - Laplace Equation, SOR
15.	L15	Laplace Equation - Final, Linear Wave Equation
16.	L 16	Linear Wave Equation - Closed Form & Numerical Solution, Stability Analysis
17.	L17	One Dimension Wave Equation - Generating A Stable Scheme & Boundary Conditions
18.	L18	Modified Equation
19.	L19	Effect Of Higher Derivative Terms On Wave Equation
20.	L20	Artificial Dissipation, Upwinding, Generating Schemes
21.	L21	Demo - Modified Equation, Wave Equation
22.	L22	Demo - Wave Equation / Heat Equation
23.	L23	Quasi-Linear One-Dimensional. Wave Equation
24.	L24	Shock Speed, Stability Analysis, Derive Governing Equations
25.	L25	One-Dimensional Euler Equations - Attempts To Decouple
26.	L26	Derive Eigenvectors, Writing Programs
27.	L27	Applying Boundary Conditions
28.	L28	Implicit Boundary Conditions
29.	L29	Flux Vector Splitting, Setup Roe's Averaging
30.	L30	Roes Averaging
31.	L31	Demo - One Dimensional Flow
32.	L32	Accelerating Convergence - Preconditioning, Dual Time Stepping
33.	L33	Accelerating Convergence, Intro to Multigrid Method

<b>34.</b>	<b>L34</b>	Multigrid Method
<b>35.</b>	<b>L35</b>	Multigrid Method - Final, Parallel Computing
<b>36.</b>	<b>L36</b>	Calculus Of Variations - Three Lemmas and A Theorem
<b>37.</b>	<b>L37</b>	Calculus of Variations - Application to Laplace Equation
<b>38.</b>	<b>L38</b>	Calculus of Variations -final & Random Walk
<b>39.</b>	<b>L39</b>	Overview and Recap of the course

**List of reference material/ books:**

Elements of CFD. M. Ramakrishna.

**Name and contact details of two referees for the course:**